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**Applied  
Mathematical  
Sciences  
5**

# **Fluid Dynamics**



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**R. von Mises  
K. O. Friedrichs**

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With 216 Illustrations



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